

## Mechanics

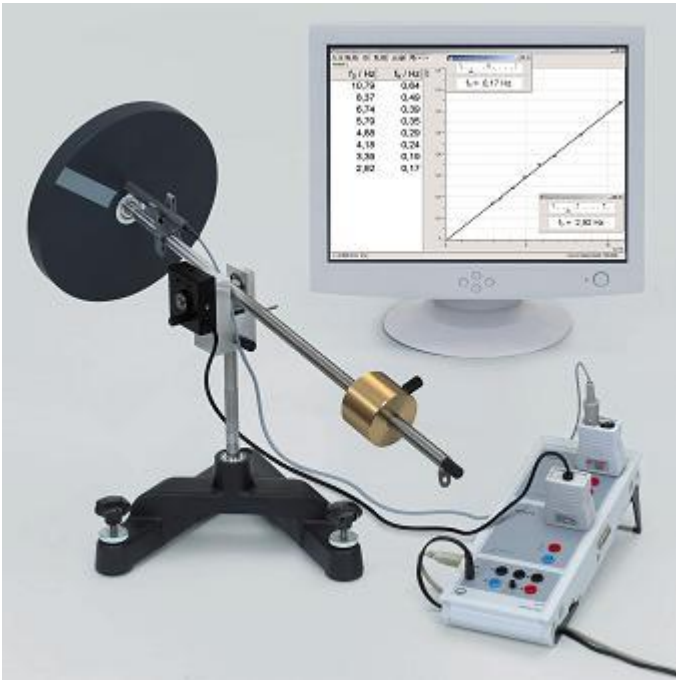
Rotational motions of a rigid body  
*Motions of a gyroscope*

## Nutation of a gyroscope

### Description from CASSY Lab 2

For loading examples and settings,  
please use the CASSY Lab 2 help.

## Gyroscope nutation



can also be carried out with [Pocket-CASSY](#)

### Principle

In the experiment, the nutation frequency  $f_N$  of a free gyroscope as a function of the rotational frequency  $f_D$  for the gyroscope disk is being investigated.

The relationship  $f_D = J_S/J_K \cdot f_N$  applies

with  $J_S = \frac{1}{2}m \cdot r^2$ : moment of inertia of the gyroscope disk about its rotational axis

and  $J_K$ : moment of inertia of the gyroscope about the gyroscope axis (point of suspension)

The moment of inertia of the gyroscope  $J_K$  is essentially the combination of the moments of inertia of the gyroscope rod  $J_1$ , the gyroscope disk  $J_2$  and the balancing mass  $J_3$  about the rotational axis.

For  $J_1$ , with the help of the parallel axes theorem:  $J_1 = m_{St}/12 \cdot l^2 + m_{St} \cdot s^2$ , applies,

with  $l$ : rod length,  $m_{St}$ : rod mass,  $s$ : distance of the gyroscope axis from the center of gravity (center) of the rod.

For  $J_2$ :  $J_2 = m_{KS} \cdot a_{KS}^2$  applies,

with  $m_{KS}$ : mass of the gyroscope disk,  $a_{KS}$ : distance from the gyroscope axis.

$J_3$  is calculated similarly (with  $m_{AM}$ : balancing mass).

### Experiment description

The nutation frequency is determined by means of a rotary motion sensor which is fitted to the gyroscope axis. In addition, the time of oscillation  $T_N$  of the vertical component of the nutation motion of the gyroscope is measured, and from this the nutation frequency  $f_N = 1/T_N$  is calculated. The rotational frequency is determined by means of the reflection light barrier. To do this, the period  $T_D$  of the rotational motion of the gyroscope disk is measured, and from this the rotational frequency  $f_D = 1/T_D$  is calculated.

### Equipment list

1	<a href="#">Sensor-CASSY</a>	524 010 or 524 013
1	<a href="#">CASSY Lab 2</a>	524 220
1	<a href="#">Rotary motion sensor S</a>	524 082
1	<a href="#">Timer S</a>	524 074
1	Reflection light barrier	337 468
1	Gyroscope	348 20


- 1 Double spring clip 590 021  
 1 PC with Windows XP/Vista/7/8

### Experiment setup (see diagram)

- Attach the reflection light barrier by means of the spring clip approx. 1 cm in front of the gyroscope disk.
- Fit the rotary motion sensor from below onto the gyroscope axis and fix with the thumb screw.
- The supply cable is to be laid in such a way that it does not exert any forces on the gyroscope and so that the gyroscope can rotate freely for at least one turn.
- Shift the balancing mass so that the gyroscope is balancing, i.e. it is free of forces.

### Carrying out the experiment

#### ■ Load settings

- Testing of the correct adjustment of the reflection light barrier  
Start the gyroscope disk by hand. The rotational frequency (approx. 1 Hz) should be displayed). If necessary, move the reflection light barrier slightly.
- Test of the correct adjustment of the rotary motion sensor  
Move the gyroscope uniformly up and down about its axis. The nutation frequency should be displayed (approx. 1 Hz).
- Start the gyroscope disk rotating rapidly by means of a piece of string. The maximum rotational frequency is approx. 10 Hz.
- Start the gyroscope nutation by gently pushing it.
- Record the measured value with .
- Start up nutation repeatedly for slowly decreasing rotational frequencies and make measurements. If necessary, the gyroscope disk may be braked somewhat.

### Evaluation

In the diagram of the nutation frequency  $f_N$  as a function of the rotational frequency  $f_D$  a straight line appears, i.e.  $f_N \propto f_D$ . The gradient of the straight line is the proportionality factor  $J_S/J_K$ ; in the example  $J_S/J_K = 0.0659$ .

With the estimated moment of inertia (with the simplifying assumption of an homogeneous and point mass)

$$J_S = \frac{1}{2}m \cdot r^2 \approx 0.010 \text{ kg} \cdot \text{m}^2 \quad (\text{with } m = 1.54 \text{ kg}, r = 11.5 \text{ cm})$$

$$J_1 = m_{St}/12 \cdot l^2 + m_{St} \cdot s^2 \approx 0.056 \text{ kg} \cdot \text{m}^2 \quad (\text{with } m_{St} = 0.50 \text{ kg}, l = 57 \text{ cm}, s = 6.6 \text{ cm})$$

$$J_2 = m_{KS} \cdot a_{KS}^2 \approx 0.056 \text{ kg} \cdot \text{m}^2 \quad (\text{with } m_{KS} = 1.54 \text{ kg}, a_{KS} = 19 \text{ cm})$$

$$J_3 = m_{AM} \cdot a_{AM}^2 \approx 0.063 \text{ kg} \cdot \text{m}^2 \quad (\text{with } m_{AM} = 1 \text{ kg}, a_{AM} = 25 \text{ cm})$$

$$J_K = J_1 + J_2 + J_3 \approx 0,136 \text{ kg} \cdot \text{m}^2$$

results in  $J_S/J_K \approx 0.074$ .